

# EFFECT OF DUCTILITY NUMBERS OF CONCRETE AND AGGREGATE ON SHEAR STRENGTH OF HIGH-STRENGTH CONCRETE MEMBERS

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## ABSTRACT

This paper describes the diagonal cracking shear behavior of reinforced high-strength concrete (HSC) members without web reinforcement. It was found that the diagonal cracking shear strength of HSC is governed by the ratio of uniaxial compressive strength to tensile strength (the ductility number,  $DN$ ) of the concrete relative to that of the aggregate. As the  $DN$  of concrete exceeded that of the aggregate, diagonal cracking shear strength decreased due to the smooth fracture surface and brittleness. Based on the  $DN$ s of concrete and aggregate, definitions for concrete strength regions were proposed.

**Keywords:** brittleness, ductility number, fracture surface, high-strength concrete, shear

## 1. INTRODUCTION

The invention of super plasticizers and other mineral additives has enabled the use of high-strength concrete (HSC) allowing for more efficient use of space and enhanced structural performance [1]. However, until now, no fundamental theory has explained how to distinguish HSC from normal strength concrete (NSC). Although there is no particular theory to explain where NSC becomes HSC, the ACI has defined HSC as concrete which has a compressive strength greater than 41 MPa [2]. Also, the use of HSC has led to some concerns about its diagonal cracking shear strength because of its brittleness and smooth fracture surface [3, 4].

Diagonal cracking shear failure of RC members without web reinforcement initiates when the principal tensile stress within the shear span exceeds the tensile strength of concrete. Also, the diagonal cracking shear strength of a reinforced concrete (RC) member without shear reinforcement is carried by the shear resistance of uncracked concrete in the compression zone, the interlocking action of aggregate (crushed and screened rock) along the concrete surfaces on each side of a crack, and the dowel action of the longitudinal reinforcement. In rectangular beams, the proportions of the shear strength carried by these mechanisms are as follows: 53-90% by the uncracked concrete in the compression zone and through aggregate interlocking, and 15-25% by dowel action [5]. That is, in RC beams without web reinforcement the shear force is mainly carried by the interlocking action of aggregate across flexural cracks and uncracked concrete in the compression zone. Both these mechanisms are dependent on concrete strength. Therefore, the diagonal cracking shear strength of RC members strongly depends on the strengths (compressive strength and

tensile strength) of concrete. Also, the strengths of the aggregate control the strengths of concrete, particularly HSC. However, a fundamental theory explaining the diagonal cracking shear strength of beams relative to aggregate strengths is still missing.

In NSC, the properties of coarse-aggregate seldom become strength-limiting, since NSC mixtures typically correspond to water-cement ratios ( $w/c$ ) in the order of 0.4 to 0.7. Within this  $w/c$  range, the weakest components in concrete are the hardened cement paste and the transition zone between the cement paste and coarse-aggregate, rather than coarse-aggregate itself [6]. However, in HSC, the hardened cement paste and the transition zone are no longer strength-limiting. This is because the concrete mixtures are usually made with a low  $w/c$  (0.2 to 0.3). On the contrary, it is the strength of the coarse-aggregate itself that controls the strength of HSC [3]. However, there is little information on the influence of coarse-aggregate characteristics on HSC strengths [7].

The fracture surface of HSC is relatively smoother than that of NSC since cracks penetrate through aggregate [8]. The effectiveness of shear transfer through aggregate interlock is commonly believed to be reduced if the coarse aggregate fractures at cracks as is frequently the case in HSCs. Until now, no theory has attempted to explain the roughness of concrete fracture surface relative to strengths of concrete and aggregate [3, 4]. It has been found that, the shear resistance of uncracked concrete in the compression zone is lower with HSC as a result of its brittleness [9].

Against this background, the objectives of this study are: 1) to quantitatively explain the effect of both concrete strength and aggregate strength on fracture surface of concrete, 2) to propose a diagonal cracking shear behavior with respect to aggregate and concrete

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strengths, and 3) to define the concrete strength regions.

## 2. DUCTILITY NUMBER ( $DN$ )

The effectiveness of shear transfer through aggregate interlock is believed to be reduced if the coarse aggregate fractures at cracks [3, 4]. Therefore, an understanding of the fracture mechanism of rock is a prerequisite for designing RC members. In fact, the study of brittle fracture forms is a fundamental research area in rock mechanics. The envelope for brittle failure is mainly determined by the peak stresses of the rock and can be determined using the Brazilian splitting tension test and uniaxial compression test [10]. Mohr's theory is often used to predict the failure of brittle materials. Therefore, the failure of rock is mostly described using Mohr's failure theory. In this study, linear Mohr's envelopes tangent to the Brazilian splitting tension tests and uniaxial compression tests were considered due to their easy application (Fig.1).

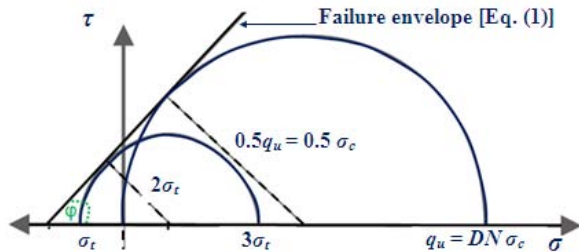


Fig.1 Mohr's failure envelope for Brazilian splitting tension test and uniaxial compression test

According to Fig.1, the failure envelope to the Brazilian tension circle and uniaxial compression circle can be expressed as follows

$$\tau = \left[ \frac{DN-4}{2\sqrt{DN-3}} \right] \sigma + \frac{q_u}{2\sqrt{DN-3}} \quad (1)$$

where,  $\tau$  is shear stress,  $\sigma$  is normal stress,  $q_u$  is compressive strength, and  $DN$  is the ductility number [that is, the ratio of uniaxial compressive strength ( $\sigma_c$ ) to tensile strength ( $\sigma_t$ )].

The value of  $DN$  can be used as a measure of material brittleness since it governs the material friction angle ( $\phi$ ) [11, 12]. Therefore, for a particular aggregate type, the value of  $DN$  can be used as a measure of concrete brittleness [3, 11, and 12]. A higher value of  $DN$  corresponds to a more brittle concrete [3]. Also, when Mohr's circles of HSC strengths reach the rupture envelope of aggregate, aggregate in HSC ruptures resulting in a smooth fracture surface. That is, the  $DN$  of concrete ( $DNC$ ) is higher than that of aggregate. The

smooth crack surface reduced aggregate interlock and lowered the shear strength of HSC members. However, this behavior should be experimentally verified.

## 3. TEST PROGRAMS

### 3.1 Materials

In this study, the diagonal cracking shear behavior was described using the  $DN$ s of concrete and aggregate. As tabulated in Table 1, twelve beams without web reinforcement were used in this study. The cross sections and layout of test beams are shown in Fig.2. The test variables were compressive strength of concrete and shear span to effective depth ( $a/d$ ) ratio.

All specimens including RC beams, compressive strength specimens ( $\Phi 100 \times 200 \text{ mm}$ ), and splitting tensile strength specimens ( $\Phi 150 \times 300 \text{ mm}$ ), were cured up to the loading test age to exclude the drying effects.

To determine the aggregate strengths, uniaxial compressive strength and tensile strength tests of rock cylinders were measured. Cylinder specimens measuring 50 mm in diameter and 100 mm in height were prepared for uniaxial compressive strength tests and others measuring 50 mm in diameter and 50 mm in height were prepared for tensile strength tests (measured using the Brazilian test). Refer to Table 2 for the results of these tests.

### 3.2 Instrumentation and Measurements

#### (1) Beam test

The four-point symmetrical loading with a distance of 300 mm between the loading points was statically applied to all specimens (Fig.2). Vertical deflections at the center, shear span and support of the RC beam were measured by displacement transducers. The test was stopped when the crushing of the concrete in compression and considerable loss of load carrying capacity was observed.

#### (2) Surface roughness index test

A laser-light confocal microscope was used to scan the fractured splitting-tensile-strength test specimens' surface three dimensionally [3, 4]. A 100 mm x 100 mm (at the center of the specimen) area of fractured surface was scanned with a 250  $\mu\text{m}$  pixel size and resolution of 0.01  $\mu\text{m}$ .

### 3.3 Roughness Index of the Fracture Surface ( $R_s$ )

The interlocking action of aggregate along a crack can be described using post-failure evidence from the fracture surface. It is commonly recognized that the roughness of the fracture surface can vary depending on concrete mix design. Until now, however, this has not been quantitatively explained [3, 4].

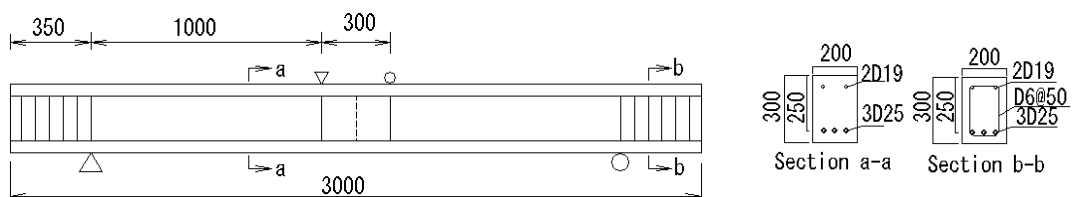


Fig.2 Details of RC beam (unit: mm)

For the surface roughness test, fractured splitting-tensile-strength test specimens were tested. The fracture surfaces of these specimens were not damaged since they failed in mode I. The roughness index ( $R_s$ ) was calculated from the directly measured surface area [3, 4] as shown by Eq. (2) (Fig.3).

$$R_s = \frac{\text{actual surface area}}{\text{projected surface area}} = \frac{\sum A_i}{\sum A} \quad (2)$$

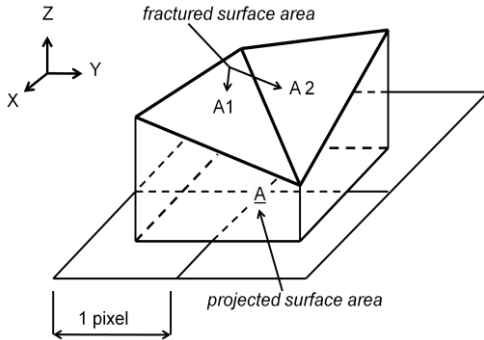


Fig.3 Schematic view of roughness parameter

Table 1 Test variables and beam test results

Specimen	$a/d$	$f'_c$ (MPa)	$f_t$ (MPa)	$V_c$ (kN)
NSC40-a	3.0	38	3.2	75.0
NSC40-b	3.5	38	3.4	78.0
NSC40-c	4.0	36	3.1	76.5
HA80	-	81	4.9	-
HA100-a	3.0	133	6.1	85.5
HA100-b	3.5	116	5.4	85.0
HA100-c	4.0	114	5.2	85.0
HA120	4.0	138	7.2	82.5
HA150	4.0	155	8.3	85.0
HA160-a	3.0	165	7.4	81.0
HA160-b	3.5	194	6.8	77.0
HA160-c	4.0	183	7.4	75.0
HA160-d	4.0	175	8.5	67.0

$a/d$ : Shear span to depth ratio

$f'_c$ : Compressive strength,  $f_t$ : Tensile strength

$V_c$ : Shear force at diagonal cracking.

## 4. RESULTS AND DISCUSSION

### 4.1 Properties of Concrete

The compressive strength and splitting tensile strength at the time of the beam test are tabulated in Table 1. The roughness index,  $R_s$ , of the fracture surface is described using the  $DN$ .

According to Table 2 and Fig.4 (a), the aggregate type (crushed granite) used in this study has a  $DN$  in the region of 18-22 due to the strength anisotropy of individual rocks [13, 14]. Therefore, the two strength measures ( $\sigma_c$ ,  $\sigma_t$ ) have maximum and minimum values that depend on the orientation of planes in the rock. Also, regarding the maximum and minimum values of  $DN$ , the maximum value is more critical because of brittleness [Eq. (1), Fig.4 (a)] [3, 4].

According to Fig.4 (a), the  $DN$  of aggregate ( $DN_A$ ) at the critical rupture envelope was 21.3. Fig.4

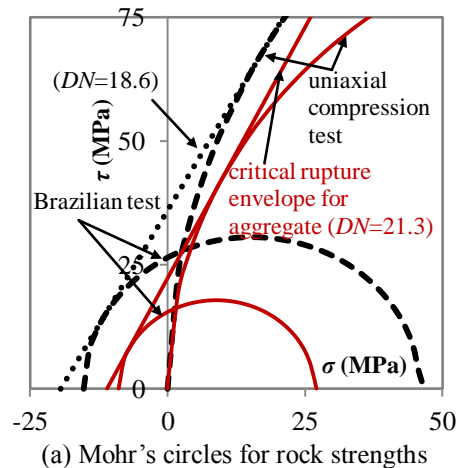
(b) explains how the fracture surfaces of HSC became smooth: Mohr's circles of concrete strengths are moving closer to the aggregate rupture envelope with an increasing  $DN$ . When Mohr's circle of NSC strengths [Fig.4 (a)  $f'_c=38$  MPa] was under the rupture envelope of aggregate, the weakest components were the hardened cement paste and the transition zone between the cement paste and coarse aggregate rather than the strength of coarse aggregate. That is, the fracture surface was rough as cracks were not penetrated through aggregate [Fig.5 (a)]. However, when Mohr's circles of HSC strengths [Fig.4 (b)  $f'_c=183$  MPa] reached the rupture envelope of aggregate, the weakest components was the strength of coarse aggregate. Therefore, aggregate in HSC ruptured with a smooth fracture surface. That is, the fracture surface of HSC was relatively smoother than that of NSC since cracks penetrate through aggregate (Fig.5).

Table 2 Properties of aggregate

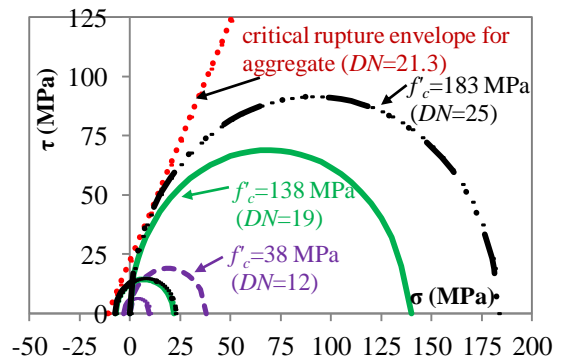
Type	$\sigma_c$ (MPa)	$\sigma_t$ (MPa)	Maximum aggregate size
Crushed granite	190-285	8.9-15.3	19 mm

$\sigma_c$ : Uniaxial compressive strength

$\sigma_t$ : Tensile strength (measured by Brazilian test)



(a) Mohr's circles for rock strengths



(b) Mohr's circles for different strengths of concrete  
Fig.4 Mohr's circles for rock and concrete

Briefly, the  $DN$  of the aggregate relative to that of concrete governs the fracture surface roughness and brittleness of concrete. Mohr's circles of concrete

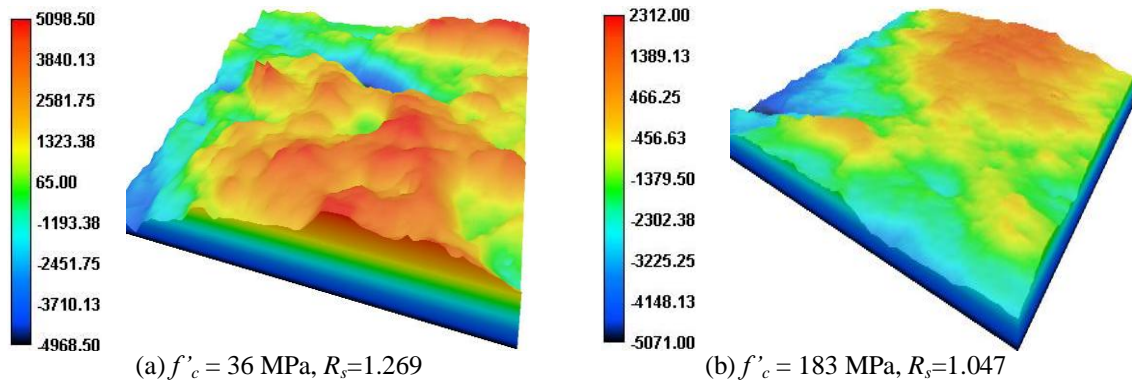


Fig.5 Fracture surface of splitting-tensile-strength test specimens,  $R_s$ : surface roughness index (color code represent the surface elevation ( $\mu\text{m}$ ))

strengths approach the aggregate rupture envelope as the  $DN$  increases. When Mohr's circles of HSC strengths pass the rupture envelope of the aggregate ( $DNC > DNA$ ), the aggregate in HSC ruptures resulting in a smooth fracture surface (Fig.6). There was a 14% reduction in  $R_s$  between concrete with a strength of 36 MPa and 114 MPa (Fig. 6). However, as concrete strength further increased from 114 MPa to 155 MPa, the change in  $R_s$  was minimal (Fig. 6) ( $DNC \approx DNA$ ). This fracture surface roughness was due to the strength anisotropy of aggregate [Fig.4 (a)]. Also, the value of  $R_s$  of HA160-d concrete with a strength of 175 MPa was the same as that of HA150 concrete with a strength of 155 MPa concrete and it was minimal due to smooth fracture surface (Fig. 6). The smooth crack surface reduced aggregate interlock and lowered the shear strength of HSC (Fig.6 and Table 1). Further, friction angle [function of  $DN$ , Eq. (1)] of concrete was increased with the increase of concrete strength. Therefore, concrete brittleness also increased with the increase of concrete  $DN$  and led to reduced shear resistance in the uncracked compression zone of HSC (Table 1).

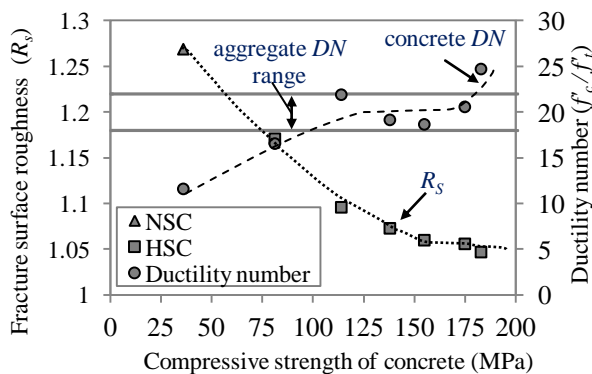


Fig.6 Fracture surface roughness of splitting-tensile-strength specimens

#### 4.2 Load-Deflection Relationship

Fig.7 shows the load-deflection curves of tested beams with  $a/d = 4.0$ . All beams exhibit similar behavior and beam HA160-c is described here as an example. In the HA160-c load-deflection curve, flexural cracks first appeared at an early stage of

loading. The load dropped slightly after formation of the first flexural crack, and then continued to rise.

The diagonal crack then occurred in the shear span and the load dropped sharply. Even though diagonal cracking took place, the beam was still able to bear the applied load through arch action. Finally the beam failed in shear compression when the diagonal cracks in the shear span widened and the concrete near the crack tip in the compression zone was crushed. Beams HA100-a, HA100-b, HA150, HA160-a, HA160-b, HA160-c, and HA160-d all failed in shear compression while all other beams, including HA120 and HA100-c, failed in diagonal tension. Diagonal tension failure occurred just after the occurrence of critical diagonal cracking.

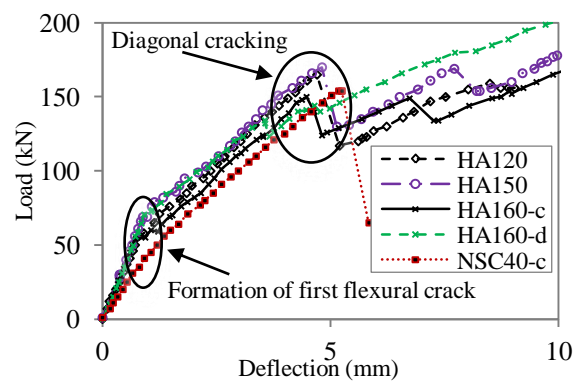


Fig.7 Comparison of load -deflection relationship of RC beams

#### 4.3 Diagonal Cracking Shear Behavior

Test results indicated that diagonal cracking shear strength of the HSC beam with a concrete strength of 114 MPa (beam HA100-c) was 11% higher than that beam in NSC40-c ( $f'_c = 36$  MPa). This increase was due to the roughness of the fracture surface ( $DNC < DNA$ ) and the 67% increase in  $f_i$ . The shear strength of HSC beams was constant for concrete strengths between 114 MPa (beam HA100-c) and 155 MPa (beam HA150). This behavior was due to the improved  $f_i$  and the  $DN$  of the concrete and aggregate being approximately equal (Fig. 6 and Fig. 8) ( $DNC \approx DNA$ ). However, the shear strength of beam

HA160-c ( $f'_c = 183$  MPa) was 12% lower than that of beam HA150 ( $f'_c = 155$  MPa) (Fig.8). This reduction was due to the smooth fracture surface (Fig. 6) and the increase in brittleness ( $DNC > DNA$ ).

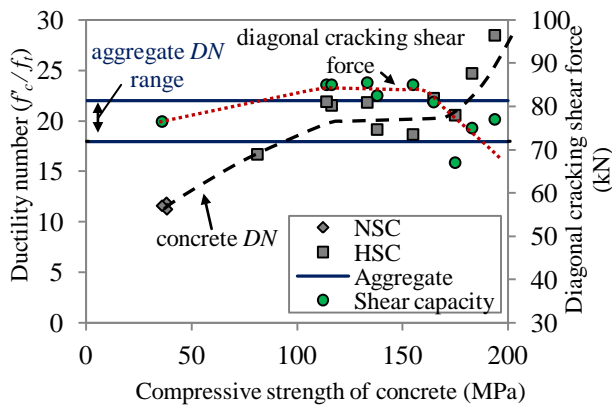


Fig.8 Effect of compressive strength of concrete on ductility number ( $DN$ ) and diagonal cracking shear force of RC beams

#### 4.4 Proposed Diagonal Cracking Shear Behavior

The  $DN$  of the concrete relative to that of the coarse aggregate governs the fracture surface roughness and brittleness of concrete and diagonal cracking shear strength of HSC. When the  $DN$  of concrete was lower than that of the aggregate, the shear strength increased with the increase of concrete strength due to rough fracture surface and increased tensile strength. When the  $DN$ s of the concrete and aggregate were equal, shear strength stayed constant at the maximum value. However, when concrete had a higher  $DN$  than the aggregate, shear strength decreased due to the smooth fracture surface and high brittleness of the concrete (Fig.9).

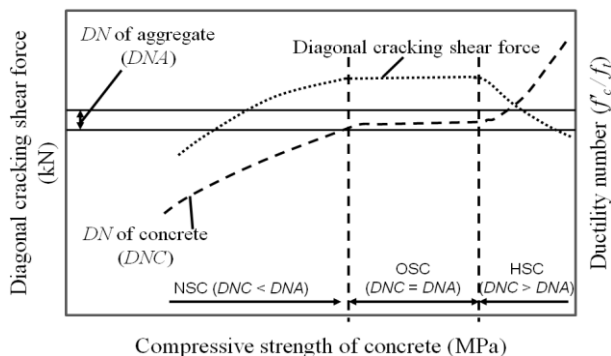


Fig.9 Effect of compressive strength of concrete on  $DN$  and diagonal cracking shear force of RC members (NSC: Normal strength concrete, OSC: Optimal strength concrete, HSC: High-strength concrete)

#### 4.5 Verification of Proposed Diagonal Cracking Shear Behavior

Until now, no research has attempted to look at the relationship between diagonal cracking shear strength and aggregate  $DN$ . Hence, no past study was available in this research area for comparison. However,

to check the validity of proposed shear failure theory, test results from two different investigators were examined [15, 16].

According to Fujita et al., research has been carried out on the  $DN$  of concrete below and above that of aggregate [15]. However, no research work has been done on the equal  $DN$  of concrete and aggregate. The studied test variables include concrete strength (36MPa-100MPa) and beam depth (250mm-1000mm) [15]. Fig.10 shows the average beam test and concrete strength results. The suggested  $DN$  for aggregate was 19 (Fig.10). In each beam depth, the shear behavior of beams of this study agreed with the predicted shear behavior for concrete  $DN$  below and above that of aggregate (Fig.10).

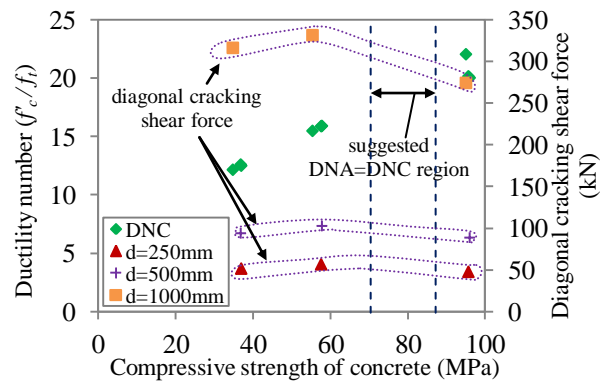


Fig.10 Test results reported by Fujita et al. [15]

Sato et al. have conducted an experiment where concrete  $DN$  was equal to that of aggregate [16]. Although no data on the aggregate was given, three aggregate types (A, B, C) were used in this study [16]. Beams with a depth of 250mm were selected to study the effect aggregate type on shear behavior (Fig.11). The suggested  $DN$ s for aggregate were 18 (A and C) and 26 (B). In each aggregate type, the shear strength of RC beams of this study stayed constant as suggested (Fig.11).

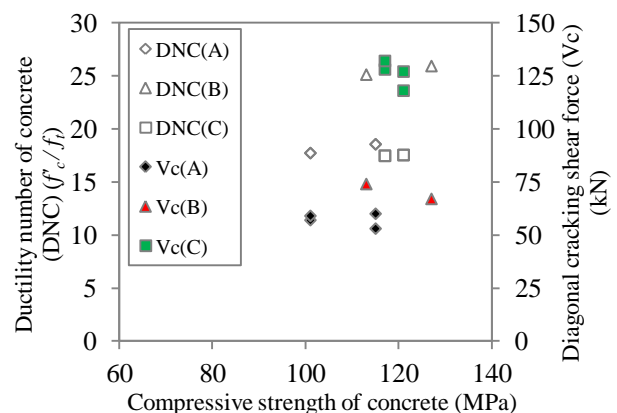


Fig.11 Test results reported by Sato et al. [16]

As mentioned above, previous to this study, no research had studied the relationship between shear strength and  $DN$ . Therefore, further studies using different aggregate sizes and rock types are essential.

#### 4.6 New Definition for Concrete Strengths

When discussing the diagonal cracking shear strengths, there is a need for well-defined concrete strength regions. Based on the above discussion, previous studies and aggregate strength variations [1-16], it is suggested that concrete can be categorized as NSC, optimal strength concrete (OSC), and HSC. These can be defined as follows (Fig.9).

(a) Normal strength concrete (NSC): The concrete compressive strength is less than optimum concrete strength. That is, in this strength region, concrete  $DN$  is lower than that of the aggregate ( $DNC < DNA$ ).

(b) Optimal strength concrete (OSC): The  $DN$  of concrete is similar that of the aggregate ( $DNC \approx DNA$ ). This strength region was proposed based on the strength anisotropy of individual rock.

(c) High strength concrete (HSC): Concrete strength exceeds the optimum concrete strength. That is, in this strength region, the concrete  $DN$  is higher than that of the aggregate ( $DNC > DNA$ ).

However, further studies on properties of NSC, OSC and HSC are important.

#### 5. CONCLUSIONS

The shear behavior of RC beams without web reinforcement was investigated. The results of a series of tests on 12 beams were presented and analyzed. Based on these results, the following conclusions can be drawn:

- (1) By considering concrete brittleness and fracture surface roughness in conjunction with the ductility numbers of concrete and coarse aggregate, designers' understanding of shear behavior will be enhanced.
- (2) The ductility number of the aggregate relative to that of concrete governs the fracture surface roughness of concrete and the shear strength of HSC. When the ductility number of concrete was lower than that of the aggregate, the shear strength increased with the increase of concrete strength due to rough fracture surface and increased tensile strength. When the ductility numbers of the concrete and aggregate were equal, shear strength stayed constant with a maximum value. However, when concrete had a higher ductility number than the aggregate, shear strength decreased due to the smooth fracture surface and high brittleness of the concrete. However, in this study, the maximum coarse aggregate size was 19 mm and the rock type was crushed granite. Therefore, further studies on different aggregate sizes and rock types are essential.
- (3) The ductility numbers of concrete relative to that of aggregate were considered and definitions for concrete strength regions were proposed.

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